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Overview

Course Description

Quantitative Analysis limits its focus to the practical application of quantitative tools for analyzing data, drawing appropriate conclusions from datasets, and presenting both the analysis and conclusions in ways that enhance communication with appraisal clients. It reviews and furthers the application of some of the basic statistical measures (mean, median, mode, standard deviation, etc.) and spends a good deal of time on linear regression analysis for use in producing and understanding various types of analyses. Central goals of the course are showing participants how to understand the reliability and validity of all data used to draw conclusions and providing the knowledge needed to check the validity of the conclusions others may draw from the same or similar datasets. Each presentation and activity demonstrates real-world appraisal applications and is aimed at furthering an appraiser’s ability to provide credible analysis of issues related to real property. The goals for the course are to help participants

- Properly apply and explain statistical methods, such as simple and multiple linear regression analysis, using market information
- Understand and critique statistical applications
- Understand how to incorporate statistical analysis in valuation reports
- Understand how to evaluate the reliability of various types of data used in valuation
- Build competence in using the language of quantitative analysis
- Use graphs to present data and analysis
- Understand research design issues such as hypothesis construction, data reliability and validity, and sampling

This course is one of a series of courses that are part of the Appraisal Institute’s Analytics for Valuation Professional Development Program. For more information about the program, see Professional Development Programs on the Appraisal Institute Web site at www.appraisalinstitute.org.

Important Notes

- **Diagnostic Test Prerequisite.** To successfully complete courses in the advanced education curriculum, it is important that participants have basic spreadsheet skills. Therefore, before enrolling in an advanced education course, each
Each course in the advanced curriculum incorporates both online and live classroom learning. A two-hour Online Session begins the course. While the content for each course is different, these Online Sessions all incorporate discussion and examples, and require participants to complete various tasks. By completing the Online Session, participants will have a better understanding of what to expect in the live classroom sessions that will follow. If the tasks are difficult, participants will have time to review and prepare before the live portion of the course begins. Tasks will not be graded; however, they must be completed to successfully pass the course. The Online Session, which goes live 28 days before the classroom session begins, must be completed BEFORE the classroom session begins.

This course incorporates a variety of interactive learning activities, including Excel datasets. Participants are required to download the necessary Excel files while completing the Online Session so that they have them when they begin the classroom portion of the course.

The Excel datasets for Quantitative Analysis may be used during the course as an aid in problem solving but also have real-world applications outside the course. Many have embedded calculations; these are for simplicity but should not be used as a crutch. It is essential that participants understand the logical and mechanical operations associated with the Excel files and not just obtain the right answer.

Learning Enhancements

The course has been designed with a variety of elements to enhance your learning experience.

- **Preview.** To give you a taste of what is to come, each Part begins with a Preview page that includes a brief overview of the content, learning objectives to consider as you move through the content, and learning tips that will assist you in understanding the information you’re about to cover.

- **Learning Objectives.** Each learning objective covers essential information for understanding the concepts in the course. Look them over before the Part begins so that you have a frame of reference as you move through the material. At the end of each Part, reread the objectives. Are you able to do what is stated? If not, this is the time to ask your instructor for help or review the concepts that you do not understand.

- **Examples and Problems.** To supplement the discussions, we’ve included examples and exercises to help you visualize and practice what you are learning.
• **Review.** Each Part concludes with a Review, which includes the learning objectives and key terms and concepts that have been covered. Also, we’ve provided recommended readings and additional practice problems from the course textbook, *An Introduction to Statistics for Appraisers*, which will reinforce what you have learned in class.

• **Practice Tests.** Practice Tests are included throughout the course. The questions are similar to the types of questions you might find on the exam. By answering these questions, you will find out whether you can apply the concepts covered.

### Classroom Guidelines

To make the course a positive experience for everyone attending, we have some guidelines for your consideration:

• 100% attendance is required. No exceptions.

• Limit use of computers and wireless devices to classroom projects.

• Communicate with business associates during break time instead of class time.

• Put away reading materials such as newspapers and books that are not used in class.

• Silence cell phones.

• Use recording devices only if prior permission has been granted.

• Refrain from ongoing conversations with those seated near you and other distracting behavior.

### General Information

• **Calculators.** A calculator is required. **Note.** Cellular phones, tablets, iPads, and other devices that connect to the Internet are NOT permitted during the exam.

• **Laptop computers.** A laptop computer is required.

• **Spreadsheet program.** *Excel 2010* is required.

• **Breaks.** There will be two 10-minute breaks during the morning session and two 10-minute breaks during the afternoon session unless noted otherwise by the course sponsor. The lunch break is one hour.

• **Attendance sheets** will be distributed during class to verify your attendance during the morning and afternoon sessions.
• **Certificates of completion** will be sent after completion of the course, and attendance during the entire course is required.

**Required Text**

• Wolverton, Marvin L., Ph.D., MAI. *An Introduction to Statistics for Appraisers*. Chicago: Appraisal Institute, 2009. (See errata list on the following page.)

**Recommended Text**


**Prerequisites**

**Required**

• *Advanced Education Diagnostic Test*

**Recommended**

• *Real Estate Finance, Statistics, and Valuation Modeling*

• *Using Spreadsheet Programs in Real Estate Appraisals—The Basics* or similar course/seminar

**Exam**

• 40 multiple-choice questions